Pratt Truss Bridge

Introduction

This example is inspired by a classic bridge type called a Pratt truss bridge. You can identify a Pratt truss by its diagonal members, which (except for the very end ones) all slant down and in toward the center of the span. All the diagonal members are subject to tension forces only, while the shorter vertical members handle the compressive forces. Since the tension removes the buckling risk, this allows for thinner diagonal members resulting in a more economic design.

A *truss structure* supports only tension and compression forces in its members and you would normally model it using bars, but as this model uses 3D beams it also includes bending moments to some extent in a *frame structure*. In the model, shell elements represent the roadway.

Model Definition

BASIC DIMENSIONS

The length of the bridge is 40 m, and the width of the roadway is 7 m. The main distance between the truss members is 5 m.

ANALYSIS TYPES

The model includes two different analyses of the bridge:

- The goal of the first analysis is to evaluate the stress and deflection fields of the bridge when exposed to a pure gravity load and also when a load corresponding to one or two trucks crosses the bridge.
- Finally, an eigenfrequency analysis shows the eigenfrequencies and eigenmodes of the bridge.

LOADS AND CONSTRAINTS

To prevent rigid body motion of the bridge, it is important to constrain it properly. All translational degrees of freedom are constrained at the left-most horizontal edge. Constraints at the right-most horizontal edge prevent it from moving in the vertical and transversal directions but allow the bridge to expand or contract in the axial



direction. This difference would however only be important if thermal expansion was studied. Figure 1 shows the bridge geometry.

Figure 1: The geometry of the bridge

The first study uses several load cases. In the first load case the effects of self weight is analyzed. The following load cases compute the solution when two trucks are moving over the bridge. The weight of each truck is 12,000 kg, the wheelbase is 6 m, the axle track is 2 m, and the weight is distributed with one third on the front axle and two thirds on the rear axle. The right side wheels of the truck are 1 m from the edge of the bridge.

In the second study the natural frequencies of the bridge are computed.

MATERIAL PROPERTIES AND CROSS SECTION DATA

The material in the frame structure is structural steel. The roadway material is concrete; the effect of reinforcement is ignored. The frame members have different cross sections:

• The main beams along the bridge have square box profiles with height 200 mm and thickness 16 mm. This also includes the outermost diagonal members.

- The diagonal and vertical members have a rectangular box section 200x100 mm, with 12.5 mm thickness. The large dimension is in the transverse direction of the bridge.
- The transverse horizontal members supporting the roadway (floor beams) are standard HEA100 profiles.
- The transverse horizontal members at the top of the truss (struts) are made from solid rectangular sections with dimension 100x25 mm. The large dimension is in the horizontal direction.

Results and Discussion

Figure 2 and Figure 3 illustrate the result. Figure 2 shows the displacements, and it can be seen that the maximum deflection amounts to 3 cm on the roadway. The distribution of axial forces (Figure 3) demonstrates the function of the frame: The interplay of members in tension and compression contribute to the load carrying function. The upper horizontal members are in compression and the lower in tension. The force in the lower members is much smaller, since the load is also shared by the roadway in this example. The diagonal members are subject to tension forces only, while the shorter vertical members handle the compressive forces.

Self weight Surface: Total displacement (m) Line: Total displacement (m)



Figure 2: Deformation under self weight.



Figure 3: The axial forces in the beams. Red is tension and blue is compression.

To study the effects of trucks moving over the bridge several load cases represent the position of the trucks, which are moved 3 m along the bridge for each load case.





Figure 4: Truck load analysis: Stresses in the bridge deck with two trucks are on the bridge.

The study of eigenfrequencies is important with respect to the excitation and frequency content from various loads such as wind loads and earthquakes.

Figure 5 shows the 9th eigenmode of the bridge, which is the fundamental mode for the roadway. The first eight eigenmodes only involve displacements of the weak members at the top of the truss.

Eigenfrequency=3.325624 Surface: Total displacement (m) Line: Total displacement (m)



Figure 5: The 9th eigenmode.

Notes About the COMSOL Implementation

You can define load cases to activate and deactivate loads within a study. All the loads need to be defined in the Model Builder. Under the Stationary Study step node, you can then select which load or constraint to activate for a specific load case. Moreover for each load case you can modify the value of the applied load by changing its weight factor.

Define load cases —										
Load case	lg1	Weight	lg2	Weight	lg3	Weight	lg4	Weight	lg5	Wei
Self Weight	×	1.0	×	1.0	×	1.0	×	1.0	×	1.0
1 truck, position 1	~	2.0	×	1.0	~	1.0	×	1.0	×	1.0
1 truck, position 2	×	1.0	~	2.0	×	1.0	~	1.0	×	1.0
1 truck, position 3	×	1.0	×	1.0	~	2.0	×	1.0	~	1.0
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When combining two different physics interfaces, they will as a default have individual sets of degrees of freedom. In structural mechanics, you will usually want them to be

equal, so you rename the displacements in the second interface to have the same name as in the first interface. In this case, where both beams and shells have rotational degrees of freedom, also these will in general need to treated. The representation of rotation is however different in the Shell and Beam interface, so the simple renaming cannot be used. In the example you can see how the rotations in the beam elements are prescribed to follow those in the shell to which they are connected. In models like this, the results will be virtually the same if the connection of rotations is omitted, as long as the mesh is reasonably fine.

Model Library path: Structural_Mechanics_Module/Civil_Engineering/ pratt_truss_bridge

Modeling Instructions

MODEL WIZARD

- I Go to the Model Wizard window.
- 2 Click Next.
- 3 In the Add physics tree, select Structural Mechanics>Shell (shell).
- 4 Click Add Selected.
- 5 In the Add physics tree, select Structural Mechanics>Beam (beam).
- 6 Click Add Selected.

Make the beam and shell elements have common displacements.

- 7 Find the Dependent variables subsection. In the Displacement field edit field, type u.
- 8 In the Displacement field components table, enter the following settings:

- 9 Click Next.
- **10** Find the **Studies** subsection. In the tree, select **Preset Studies for Selected Physics>Stationary**.
- II Click Finish.

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v

w

GLOBAL DEFINITIONS

Parameters

- I In the Model Builder window, right-click Global Definitions and choose Parameters.
- 2 In the Parameters settings window, locate the Parameters section.

3 In the table, enter the following settings:

Name	Expression	Description
width	7[m]	Width of bridge
height	5[m]	Height of bridge
spacing	5[m]	Spacing between members along the bridge
length	40[m]	Total bridge length
truck_weight	12000[kg]	Total truck weight

4 Right-click **Global Definitions** and choose **Load Group**. Repeat this nine times so that you get ten load groups.

GEOMETRY I

In the Model Builder window, under Model I right-click Geometry I and choose Work Plane.

Plane Geometry

Create the bridge deck.

Rectangle 1

- I In the Model Builder window, under Model I>Geometry I>Work Plane I right-click Plane Geometry and choose Rectangle.
- 2 In the Rectangle settings window, locate the Size section.
- 3 In the Width edit field, type spacing.
- 4 In the **Height** edit field, type width.
- 5 Locate the **Position** section. In the **xw** edit field, type -length/2.
- 6 Click the **Build All** button.

Array I

- I Right-click Plane Geometry and choose Transforms>Array.
- 2 In the Array settings window, locate the Size section.
- 3 From the Array type list, choose Linear.

- 4 Select the object rl only.
- **5** In the **Size** edit field, type length/spacing.
- 6 Locate the **Displacement** section. In the **xw** edit field, type **spacing**.
- **7** Click the **Build All** button.
- 8 Click the **Zoom Extents** button on the Graphics toolbar.

Plane Geometry

Make it possible to create beams along the edges.

Convert to Curve 1

- I Right-click Plane Geometry and choose Conversions>Convert to Curve.
- 2 In the Convert to Curve settings window, locate the Input section.
- **3** Select the **Keep input objects** check box.
- **4** Click in the **Graphics** window, press Ctrl+A to highlight all objects, and then right-click to confirm the selection.
- 5 Click the Build All button.
- 6 In the Model Builder window, right-click Geometry I and choose Build All.
- 7 Click the **Zoom Extents** button on the Graphics toolbar.

Start creating the truss.

Work Plane 2

- I Right-click Geometry I and choose Work Plane.
- 2 In the Work Plane settings window, locate the Work Plane section.
- 3 From the Plane list, choose xz-plane.

Bézier Polygon I

- I In the Model Builder window, under Model I>Geometry I>Work Plane 2 right-click Plane Geometry and choose Bézier Polygon.
- 2 In the Bézier Polygon settings window, locate the General section.
- **3** From the **Type** list, choose **Open curve**.
- 4 Locate the Polygon Segments section. Find the Added segments subsection. Click the Add Linear button.
- 5 Find the Control points subsection. In row 2, set xw to spacing.
- 6 In row 2, set yw to height.
- 7 Find the Added segments subsection. Click the Add Linear button.

- 8 Find the Control points subsection. In row 2, set yw to 0.
- 9 Click the **Build All** button.

Bézier Polygon 2

- I Right-click Plane Geometry and choose Bézier Polygon.
- 2 In the Bézier Polygon settings window, locate the General section.
- **3** From the **Type** list, choose **Open curve**.
- 4 Locate the **Polygon Segments** section. Find the **Added segments** subsection. Click the **Add Linear** button.
- 5 Find the **Control points** subsection. In row I, set **yw** to height.
- 6 In row 2, set xw to spacing.
- 7 In row 2, set yw to height.
- 8 Click the Build All button.

Array I

- I Right-click Plane Geometry and choose Transforms>Array.
- 2 In the Array settings window, locate the Size section.
- 3 From the Array type list, choose Linear.
- 4 Select the objects **b1** and **b2** only.
- 5 In the Size edit field, type length/(2*spacing)-1.
- 6 Locate the **Displacement** section. In the xw edit field, type spacing.
- 7 Click the **Build All** button.

Bézier Polygon 3

- I Right-click Plane Geometry and choose Bézier Polygon.
- 2 In the Bézier Polygon settings window, locate the General section.
- 3 From the Type list, choose Open curve.
- 4 Locate the **Polygon Segments** section. Find the **Added segments** subsection. Click the **Add Linear** button.
- 5 Find the Control points subsection. In row I, set xw to length/2-spacing.
- 6 In row I, set yw to height.
- 7 In row 2, set xw to length/2.
- 8 Click the Build All button.

Mirror I

- I Right-click Plane Geometry and choose Transforms>Mirror.
- **2** Click in the **Graphics** window, press Ctrl+A to highlight all objects, and then right-click to confirm the selection.
- 3 In the Mirror settings window, locate the Input section.
- 4 Select the Keep input objects check box.
- **5** Click the **Build All** button.
- 6 Click the Zoom Extents button on the Graphics toolbar.

Bézier Polygon 4

- I Right-click Plane Geometry and choose Bézier Polygon.
- 2 In the Bézier Polygon settings window, locate the General section.
- 3 From the Type list, choose Open curve.
- 4 Locate the Polygon Segments section. Find the Added segments subsection. Click the Add Linear button.
- 5 Find the Control points subsection. In row 2, set yw to height.
- 6 Click the **Build All** button.
- 7 In the Model Builder window, right-click Geometry I and choose Build All.

Сору І

- I Right-click Geometry I and choose Transforms>Copy.
- 2 In the Copy settings window, locate the Displacement section.
- 3 In the y edit field, type width.
- 4 Select all edges that are not part of the bridge deck. (wp2.arr1(1,2), wp2.arr1(3,1), wp2.arr1(2,1), wp2.arr1(1,1), wp2.mir1(1), wp2.b3, wp2.arr1(3,2), wp2.arr1(2,2), wp2.mir1(6), wp2.mir1(7), wp2.b4, wp2.mir1(2), wp2.mir1(3), wp2.mir1(4), and wp2.mir1(5)).
- **5** Click the **Build All** button.

Bézier Polygon I

- I Right-click Geometry I and choose More Primitives>Bézier Polygon.
- 2 In the Bézier Polygon settings window, locate the Polygon Segments section.
- **3** Find the **Added segments** subsection. Click the **Add Linear** button.
- 4 Find the **Control points** subsection. In row I, set x to -length/2+spacing.
- 5 In row I, set z to height.

- 6 In row 2, set x to -length/2+spacing.
- 7 In row 2, set y to width.
- 8 In row 2, set z to height.
- **9** Click the **Build All** button.

Array I

- I Right-click Geometry I and choose Transforms>Array.
- 2 Select the object **b1** only.
- 3 In the Array settings window, locate the Size section.
- 4 From the Array type list, choose Linear.
- **5** Locate the **Displacement** section. In the **x** edit field, type **spacing**.
- 6 Locate the Size section. In the Size edit field, type length/spacing-1.

Create points in the positions where the loads from the truck wheels are to be applied.

Point I

- I Right-click Geometry I and choose More Primitives>Point.
- 2 In the **Point** settings window, locate the **Point** section.
- 3 In the x edit field, type -19.
- **4** In the **y** edit field, type 1.

Array 2

- I Right-click Geometry I and choose Transforms>Array.
- 2 Select the object **pt1** only.
- 3 In the Array settings window, locate the Size section.
- **4** In the **x size** edit field, type 10.
- **5** In the **y size** edit field, type 2.
- 6 Locate the **Displacement** section. In the **x** edit field, type **3**.
- 7 In the y edit field, type 2.
- 8 Click the Build All button.

DEFINITIONS

Create groups for the different beam sections.

Box I

I In the Model Builder window, under Model I right-click Definitions and choose Selections>Box.

- 2 In the Box settings window, locate the Geometric Entity Level section.
- 3 From the Level list, choose Edge.
- **4** Locate the **Box Limits** section. In the **x minimum** edit field, type (length/2+1).
- 5 In the x maximum edit field, type length/2+1.
- 6 In the **y minimum** edit field, type 1.
- 7 In the **y maximum** edit field, type width-1.
- 8 In the z minimum edit field, type -1.
- 9 In the **z maximum** edit field, type 1.
- **IO** Right-click **Model I>Definitions>Box I** and choose **Rename**.
- II Go to the **Rename Box** dialog box and type BeamsTransvBelow in the **New name** edit field.

12 Click OK.

Box 2

- I Right-click Definitions and choose Selections>Box.
- 2 In the Box settings window, locate the Geometric Entity Level section.
- **3** From the **Level** list, choose **Edge**.
- 4 Locate the Box Limits section. In the x minimum edit field, type (length/2+1).
- 5 In the x maximum edit field, type length/2+1.
- 6 In the **y minimum** edit field, type 1.
- 7 In the **y maximum** edit field, type width-1.
- 8 In the z minimum edit field, type height-1.
- 9 In the z maximum edit field, type height+1.
- IO Right-click Model I>Definitions>Box 2 and choose Rename.
- II Go to the **Rename Box** dialog box and type BeamsTransvAbove in the **New name** edit field.

12 Click OK.

Box 3

- I Right-click Definitions and choose Selections>Box.
- 2 In the Box settings window, locate the Geometric Entity Level section.
- **3** From the **Level** list, choose **Edge**.
- 4 Locate the Box Limits section. In the x minimum edit field, type (length/ 2-spacing+1).

- 5 In the x maximum edit field, type length/2-spacing+1.
- 6 In the **y minimum** edit field, type -1.
- 7 In the **y maximum** edit field, type width+1.
- 8 In the **z minimum** edit field, type 1.
- 9 In the z maximum edit field, type 2.
- **IO** Right-click **Model I>Definitions>Box 3** and choose **Rename**.
- II Go to the **Rename Box** dialog box and type BeamsDiag in the **New name** edit field.

I2 Click OK.

- **I3** Right-click **Definitions** and choose **Selections>Explicit**.
- 14 In the Explicit settings window, locate the Input Entities section.
- **I5** From the **Geometric entity level** list, choose **Edge**.
- I6 Select the All edges check box.

Difference I

- I Right-click **Definitions** and choose **Selections>Difference**.
- 2 In the Difference settings window, locate the Geometric Entity Level section.
- 3 From the Level list, choose Edge.
- 4 Locate the Input Entities section. Under Selections to add, click Add.
- 5 Go to the Add dialog box.
- 6 In the Selections to add list, select Explicit I.
- 7 Click the **OK** button.
- 8 In the Difference settings window, locate the Input Entities section.
- 9 Under Selections to subtract, click Add.
- **IO** Go to the **Add** dialog box.
- II In the Selections to subtract list, choose BeamsTransvBelow, BeamsTransvAbove, and BeamsDiag.
- I2 Click the OK button.
- **I3** In the **Model Builder** window, right-click **Difference I** and choose **Rename**.
- **I4** Go to the **Rename Difference** dialog box and type BeamsMain in the **New name** edit field.
- I5 Click OK.

MODEL I

Add the materials.

MATERIALS

Material Browser

- I In the Model Builder window, under Model I right-click Materials and choose Open Material Browser.
- 2 In the Material Browser window, locate the Materials section.
- 3 In the tree, select Built-In>Concrete.
- 4 Right-click and choose Add Material to Model from the menu.
- 5 In the Model Builder window, right-click Materials and choose Open Material Browser.
- 6 In the Material Browser window, locate the Materials section.
- 7 In the tree, select Built-In>Structural steel.
- 8 Right-click and choose Add Material to Model from the menu.

Structural steel

- I In the Model Builder window, under Model I>Materials click Structural steel.
- 2 In the Material settings window, locate the Geometric Entity Selection section.
- **3** From the **Geometric entity level** list, choose **Edge**.
- 4 From the Selection list, choose All edges.

SHELL

- I In the Model Builder window, under Model I click Shell.
- 2 In the Shell settings window, locate the Thickness section.
- **3** In the d edit field, type 0.25.

Add self weight for the bridge deck.

Body Load I

- I In the Model Builder window, right-click Shell and choose Body Load.
- 2 In the Body Load settings window, locate the Force section.
- **3** In the \mathbf{F}_{V} table, enter the following settings:

0	x
0	у
-g_const*shell.rho	z

4 Locate the Boundary Selection section. From the Selection list, choose All boundaries.

Set the boundary conditions of the bridge.

Pinned I

- I Right-click Shell and choose Pinned.
- **2** Select Edge 1 only.

Prescribed Displacement/Rotation 11

- I Right-click Shell and choose Prescribed Displacement/Rotation.
- 2 Select Edge 78 only.
- **3** In the **Prescribed Displacement/Rotation** settings window, locate the **Prescribed Displacement** section.
- 4 Select the Prescribed in y direction check box.
- **5** Select the **Prescribed in z direction** check box.

Add the possible loads from the truck wheels.

Point Load 1

- I Right-click Shell and choose Points>Point Load.
- 2 In the Model Builder window, under Model I>Shell right-click Point Load I and choose Load Group>Load Group I.
- 3 In the Model Builder window, click Point Load I.
- 4 Select Points 3 and 4 only.
- 5 In the Point Load settings window, locate the Force section.
- **6** In the \mathbf{F}_{p} table, enter the following settings:

0	x
0	у
-truck_weight*g_const/6	z

Point Load 2

- I Right-click Point Load I and choose Duplicate.
- 2 In the Model Builder window, under Model I>Shell right-click Point Load 2 and choose Load Group>Load Group 2.
- 3 In the Point Load settings window, locate the Point Selection section.
- 4 Click Clear Selection.
- 5 Select Points 5 and 6 only.

Point load	Points	Load group
Point Load 3	11, 12	Load Group 3
Point Load 4	15, 16	Load Group 4
Point Load 5	19, 20	Load Group 5
Point Load 6	25, 26	Load Group 6
Point Load 7	27, 28	Load Group 7
Point Load 8	33, 34	Load Group 8
Point Load 9	37, 38	Load Group 9
Point Load 10	41, 41	Load Group 10

Repeat this duplication procedure so that you get nine **Point Load** features. The loaded points and corresponding load groups are summarized in the table below:

Make the beam and shell elements have equal rotations.

BEAM

Prescribed Displacement/Rotation 11

- I In the Model Builder window, under Model I right-click Beam and choose More>Prescribed Displacement/Rotation.
- **2** In the **Prescribed Displacement/Rotation** settings window, locate the **Edge Selection** section.
- 3 From the Selection list, choose BeamsTransvBelow.
- 4 Locate the Prescribed Rotation section. Select the Prescribed in x direction check box.
- **5** Select the **Prescribed in y direction** check box.
- 6 Select the Prescribed in z direction check box.
- 7 In the θ_{0x} edit field, type shell.thx.
- **8** In the θ_{0v} edit field, type shell.thy.

Prescribed Displacement/Rotation 12

- I In the Model Builder window, right-click Beam and choose More>Prescribed Displacement/Rotation.
- 2 In the Prescribed Displacement/Rotation settings window, locate the Prescribed Displacement section.
- 3 Select the Prescribed in x direction check box.
- 4 Select the Prescribed in y direction check box.

- **5** Select the **Prescribed in z direction** check box.
- 6 Locate the Prescribed Rotation section. Select the Prescribed in x direction check box.
- **7** Select the **Prescribed in y direction** check box.
- 8 Select the Prescribed in z direction check box.
- **9** In the θ_{0x} edit field, type shell.thx.
- **IO** In the θ_{0y} edit field, type shell.thy.
- II Select Edge 1 only.

Prescribed Displacement/Rotation 13

- I Right-click Beam and choose More>Prescribed Displacement/Rotation.
- 2 In the Prescribed Displacement/Rotation settings window, locate the Prescribed Displacement section.
- **3** Select the **Prescribed in y direction** check box.
- 4 Select the Prescribed in z direction check box.
- 5 Locate the Prescribed Rotation section. Select the Prescribed in x direction check box.
- 6 Select the Prescribed in y direction check box.
- 7 Select the Prescribed in z direction check box.
- **8** In the θ_{0x} edit field, type shell.thx.
- **9** In the θ_{0v} edit field, type shell.thy.
- IO Select Edge 78 only.

Set the cross-section data of the different beam types.

Cross Section Data 1

- I In the Model Builder window, under Model I>Beam click Cross Section Data I.
- 2 In the Cross Section Data settings window, locate the Cross Section Definition section.
- **3** From the list, choose **Common sections**.
- 4 From the Section type list, choose Box.
- **5** In the h_v edit field, type 200[mm].
- 6 In the h_z edit field, type 200[mm].
- 7 In the t_v edit field, type 16[mm].
- 8 In the t_z edit field, type 16[mm].
- 9 Right-click Model I>Beam>Cross Section Data I and choose Rename.

10 Go to the **Rename Cross Section Data** dialog box and type **Cross Section Main** in the **New name** edit field.

II Click OK.

Section Orientation 1

- I In the Section Orientation settings window, locate the Section Orientation section.
- 2 From the Orientation method list, choose Orientation vector.
- **3** In the *V* table, enter the following settings:

0	x
1	у
0	z

Cross Section Data 2

I In the Model Builder window, right-click Beam and choose Cross Section Data.

2 In the Cross Section Data settings window, locate the Edge Selection section.

- 3 From the Selection list, choose BeamsDiag.
- **4** Locate the **Cross Section Definition** section. From the list, choose **Common sections**.
- 5 From the Section type list, choose Box.
- 6 In the h_v edit field, type 200[mm].
- 7 In the h_z edit field, type 100[mm].
- 8 In the t_v edit field, type 12.5[mm].
- **9** In the t_z edit field, type 12.5[mm].
- **IO** Right-click **Model I>Beam>Cross Section Data 2** and choose **Rename**.
- II Go to the Rename Cross Section Data dialog box and type Cross Section Diagonals in the New name edit field.
- I2 Click OK.

Section Orientation 1

- I In the Section Orientation settings window, locate the Section Orientation section.
- 2 From the Orientation method list, choose Orientation vector.
- **3** In the V table, enter the following settings:
- 0 x
- 1 y 0 z
- -

Cross Section Data 3

- I In the Model Builder window, right-click Beam and choose Cross Section Data.
- 2 In the Cross Section Data settings window, locate the Edge Selection section.
- 3 From the Selection list, choose BeamsTransvBelow.
- **4** Locate the **Cross Section Definition** section. From the list, choose **Common sections**.
- 5 From the Section type list, choose H-profile.
- 6 In the h_v edit field, type 96[mm].
- 7 In the h_z edit field, type 100[mm].
- 8 In the t_v edit field, type 8[mm].
- **9** In the t_z edit field, type 5[mm].
- IO Right-click Model I>Beam>Cross Section Data 3 and choose Rename.
- II Go to the Rename Cross Section Data dialog box and type Cross Section Transv Below in the New name edit field.

I2 Click OK.

Section Orientation 1

- I In the Section Orientation settings window, locate the Section Orientation section.
- 2 From the Orientation method list, choose Orientation vector.
- **3** In the *V* table, enter the following settings:

0	x
0	у
1	z

Cross Section Data 4

- I In the Model Builder window, right-click Beam and choose Cross Section Data.
- 2 In the Cross Section Data settings window, locate the Edge Selection section.
- 3 From the Selection list, choose BeamsTransvAbove.
- 4 Locate the Cross Section Definition section. From the list, choose Common sections.
- **5** In the h_v edit field, type 100[mm].
- 6 In the h_z edit field, type 25[mm].
- 7 Right-click Model I>Beam>Cross Section Data 4 and choose Rename.
- 8 Go to the Rename Cross Section Data dialog box and type Cross Section Transv Above in the New name edit field.

9 Click OK.

Section Orientation 1

I In the Section Orientation settings window, locate the Section Orientation section.

2 From the Orientation method list, choose Orientation vector.

3 In the *V* table, enter the following settings:

1	x
0	у
0	z

Add the self weight of the beams.

Edge Load I

- I In the Model Builder window, right-click Beam and choose Edge Load.
- 2 In the Edge Load settings window, locate the Edge Selection section.
- 3 From the Selection list, choose All edges.
- **4** Locate the Force section. From the Load type list, choose Edge load defined as force per unit volume.
- **5** In the **F** table, enter the following settings:



MESH I

- I In the Model Builder window, under Model I click Mesh I.
- 2 In the Mesh settings window, locate the Mesh Settings section.
- **3** From the **Element size** list, choose **Extremely fine**.
- 4 Click the **Build All** button.

STUDY I

Step 1: Stationary

- I In the Model Builder window, under Study I click Step I: Stationary.
- 2 In the Stationary settings window, click to expand the Study Extensions section.
- **3** Select the **Define load cases** check box.

4 Click Add.

5 In the table, enter the following settings:

Load case

Self Weight

6 Click Add.

7 In the table, enter the following settings:

Load case	lgl	Weight	lg3
1 truck, position 1	\checkmark	2.0	\checkmark

8 In a similar way, add seven more load cases with the properties given in the table below:

Load case	Active load groups and weights
1 truck, position 2	lg2: 2.0; lg4: 1.0
1 truck, position 3	lg3: 2.0; lg5: 1.0
1 truck, position 4	lg4: 2.0; lg6: 21.0
2 trucks, position 1	lg1: 1.0; lg5: 2.0; lg7: 1.0
2 trucks, position 2	lg2: 1.0; lg6: 2.0; lg8: 1.0
2 trucks, position 3	lg1: 2.0; lg3: 1.0; lg7: 2.0; lg9: 1.0
2 trucks, position 4	lg2: 2.0; lg4: 1.0; lg8: 2.0; lg10: 1.0

9 In the Model Builder window, right-click Study I and choose Compute.

RESULTS

The default plot is the stress plot for the shells using the last load case. Add a new plot containing both shell and beam results, and examine the self weight load case.

3D Plot Group 10

- I In the Model Builder window, right-click Results and choose 3D Plot Group.
- 2 In the 3D Plot Group settings window, locate the Data section.
- 3 From the Load case list, choose Self Weight.
- 4 Right-click Results>3D Plot Group 10 and choose Surface.
- 5 Right-click Results>3D Plot Group 10>Surface 1 and choose Deformation.
- 6 Right-click Results>3D Plot Group 10 and choose Line.
- 7 In the Model Builder window, under Results>3D Plot Group 10 click Line 1.

8 In the Line settings window, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Beam>Displacement>Total displacement (beam.disp).

You can indicate the dimensions of the beams by drawing them with a size depending on the radius of gyration.

9 Locate the Coloring and Style section. From the Line type list, choose Tube.

IO In the **Tube radius expression** edit field, type mod1.beam.rgy+mod1.beam.rgz.

- II Click to expand the Inherit Style section. From the Plot list, choose Surface I.
- 12 In the Model Builder window, under Results>3D Plot Group 10 click Surface 1.
- **I3** In the **Surface** settings window, click to expand the **Range** section.
- **I4** Select the **Manual color range** check box.
- **I5** In the **Maximum** edit field, type 0.05.
- **I6** In the **Model Builder** window, under **Results>3D Plot Group 10** right-click **Line I** and choose **Deformation**.
- **I7** Click the **Plot** button.
- **18** In the **3D Plot Group** settings window, locate the **Plot Settings** section.
- **I9** Clear the **Plot data set edges** check box.
- **20** Click the **Plot** button.
- 21 In the Model Builder window, under Results>3D Plot Group 10 click Line 1.
- 22 In the Line settings window, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Beam>Section forces>Local axial force (beam.Nxl).
- 23 In the Model Builder window, under Results>3D Plot Group 10 click Line 1.
- 24 In the Line settings window, locate the Inherit Style section.
- **25** From the **Plot** list, choose **None**.
- **26** Click to expand the **Range** section. Select the **Manual color range** check box.
- **27** In the **Minimum** edit field, type -9e5.
- 28 In the Maximum edit field, type 9e5.
- **29** Locate the **Coloring and Style** section. From the **Color table** list, choose **Wave**.
- **30** In the Model Builder window, under Results>**3D** Plot Group **10** right-click Surface **I** and choose Disable.

You can also look at the stress results for the different load cases including the truck weight.

Stress Top (shell)

- I In the Model Builder window, under Results click Stress Top (shell).
- 2 In the 3D Plot Group settings window, locate the Data section.
- 3 From the Load case list, choose 2 trucks, position 4.
- **4** Click the **Plot** button.

Create an animation of the trucks passing the bridge.

5 Click the Player button on the main toolbar.

You can easily remove unused plots to clean up the structure in the **Results** tree. An alternative could have been to deselect **Generate default plots** in the Study feature, but then you would have needed to create the current plot manually.

6 In the Model Builder window, select Results>Stress Bottom (shell) I, hold down the Shift key, and then select Results>Torsion Moment (beam) I. Right click and choose Delete.

ROOT

In the Model Builder window, right-click the root node and choose Add Study.

MODEL WIZARD

- I Go to the Model Wizard window.
- 2 Find the Studies subsection. In the tree, select Preset Studies for Selected Physics>Eigenfrequency.
- 3 Click Finish.

STUDY 2

Step 1: Eigenfrequency

- I In the Model Builder window, under Study 2 click Step I: Eigenfrequency.
- 2 In the Eigenfrequency settings window, locate the Study Settings section.
- **3** In the **Desired number of eigenfrequencies** edit field, type **12**.
- 4 In the Model Builder window, right-click Study 2 and choose Compute.

Select the first mode involving the roadway.

RESULTS

Mode Shape (shell)

I In the Model Builder window, under Results click Mode Shape (shell).

- 2 In the 3D Plot Group settings window, locate the Data section.
- 3 From the Eigenfrequency list, choose 3.325624.
- 4 In the Model Builder window, expand the Mode Shape (shell) node.

Mode Shape (beam)

In the Model Builder window, expand the Results>Mode Shape (beam) node.

Mode Shape (shell)

- I Right-click Line I and choose Copy.
- 2 In the Model Builder window, under Results right-click Mode Shape (shell) and choose Paste Line.
- 3 In the Line settings window, locate the Inherit Style section.
- 4 From the Plot list, choose Surface 1.
- 5 In the Model Builder window, expand the Results>Mode Shape (shell)>Surface I node, then click Deformation.
- 6 In the Deformation settings window, locate the Scale section.
- 7 Select the Scale factor check box.
- 8 In the associated edit field, type 0.2.
- 9 In the Model Builder window, under Results>Mode Shape (shell) click Surface 1.
- 10 In the Surface settings window, locate the Range section.
- II Select the Manual color range check box.
- **12** In the **Maximum** edit field, type 4.
- **I3** Click the **Plot** button.

Solved with COMSOL Multiphysics 4.3a